## TAKING INTO ACCOUNT CONSTRUCTION PARAMETERS OF CRANKSHAFT WHEN EVALUATING CHARACTERISTICS OF ITS EQUIVALENT TORSION SCHEME

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Abstract. The article is devoted to determine the parameters of the equivalent torsional scheme of the crankshaft of automotive internal combustion engines. The parameters that depend on the design features of the studied engines include the number and moments of inertia of the motor masses, the stiffness of the shaft sections and their length. Currently used methods are based on empirical data and require their identification for each specific model of the engine under study. To improve the adequacy of the data obtained, it is necessary to conduct full-scale tests of the crankshafts for stiffness. Modeling the spatial structure of the crankshaft by finite elements with further determination of the studied parameters, although it facilitates the task, requires subsequent mandatory verification of the model used. To unify the calculation methods and reduce their complexity, it is proposed to consider the elastic-deformable section of the crankshaft, taking into account the geometric parameters. The accuracy of the results obtained depends on the curve equations describing the elastic deformation surface of the crankshaft transition sections. A preliminary evaluation of the crankshaft parameters can be performed on a piecewise linear surface. Reducing the sampling step increases the accuracy of the necks, the presence of cavities inside the main and connecting rod necks. The proposed method can be used for automate crankshaft calculations of modern automotive internal combustion engines.

Keywords: crankpin, crankshaft; equivalent torsion scheme; stiffness; elastic deformation.

#### Introduction

The operation of high-forced automotive internal combustion engines is accompanied by the appearance of torsional vibrations of the crankshafts, which leads to a decrease in its effective performance, a deterioration in the emission parameters and a decrease in the resource. The final stage of creating such engines is to calculate the crankshafts for torsional vibrations and take constructive measures to reduce their negative impact [1; 2]. Therefore, the correct choice of the design scheme of the crankshaft for torsional vibrations and a reasonable calculation method determine the adequacy of the results obtained.

#### Materials and methods

In accordance with the standard methodology, the choice of the design scheme depends on the number of motor masses and the accuracy requirements of the calculation results [3]. Bringing the engine dynamic system down to determining the reduced length of individual sections of the crankshaft, i.e. the lengths of the corresponding sections of the rectilinear shaft having the same torsional stiffness as the sections of the real shaft (Fig. 1).

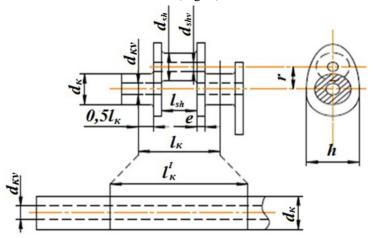


Fig. 1. Crankshaft with hollow necks

The reduced shaft elbow length is calculated according to semi-empirical formulas obtained by introducing experimental coefficients into formulas based on simplified theoretical considerations.

Let us compare the results of applying the formulas and the effect of the calculated parameters of the crankshaft on the calculated data.

For automobile engines, close to reality results are obtained when calculating the reduced knee length using the Zimanenko formula [4]. Further, the distance between the motor masses determined by this formula will be denoted as  $l'_{kol}(9)$ .

For a crankshaft with hollow necks, the formula looks like

$$l_{kol}^{'} = \left(l_{k} + 0.6\frac{e}{l_{k}} \cdot d_{k}\right) + \left(0.8 \cdot l_{sh} + 0.2 \cdot \frac{e}{r} \cdot d_{k}\right) \cdot \frac{d_{k}^{4} - d_{kv}^{4}}{d_{sh}^{4} - d_{shv}^{4}} + \frac{r\sqrt{r}}{\sqrt{d_{sh}}} \cdot \frac{d_{k}^{4} - d_{kv}^{4}}{e \cdot h^{3}},$$
(1)

where  $d_k$  – diameter of the crankshaft main journal, m;

 $d_{kv}$  – diameter of the inner shaft cavity of the crankshaft main journal, m;

 $d_{sh}$  – crankpin journal diameter, m;

 $d_{shv}$  – diameter of the inner shaft cavity of the crankshaft crankpin journal, m;

 $l_{sh}$  – crankpin journal length, m;

 $l_k$  – length of the crankshaft main journal, m;

- e thickness of the cheek, m;
- h width of the cheek, m;
- r radius of the crank, m.

For a crankshaft with solid necks ( $d_{kv} = 0, d_{shv} = 0$ )

$$l_{kol}'(9) = \left(l_k + 0.6\frac{e}{l_k} \cdot d_k\right) + \left(0.8 \cdot l_{sh} + 0.2 \cdot \frac{e}{r} \cdot d_k\right) \cdot \frac{d_k^4}{d_{sh}^4} + \frac{r\sqrt{r}}{\sqrt{d_{sh}}} \cdot \frac{d_k^4}{e \cdot h^3}.$$
 (2)

The formula of the Kolomna plant – for the shafts of engines of medium and higher power. The distance between engine masses determined by this formula will be denoted as  $l'_{kol}(10)$ .

$$l_{kol}'(10) = \frac{l_k}{d_k^4 - d_{kv}^4} + \frac{l_{sh}}{d_{sh}^4 - d_{shv}^4} + \frac{l_{sh}}{d_{sh}^4 - d_{shv}^4} + 1.8 \cdot \frac{r}{2 \cdot e \cdot h^3} \left( 1 + \frac{0.64}{r^2} \cdot \sqrt[3]{\frac{(d_k^4 - d_{kv}^4)(d_{sh}^4 - d_{shv}^4)}{r^2}} \right).$$
(3)

Carter formula – for shafts of light high-speed engines [4]. The distance between engine masses determined by this formula will be denoted as  $l'_{kol}(11)$ 

$$l'_{kol}(11) = \frac{l_k + 0.8 \cdot e}{d_k^4 - d_{kv}^4} + \frac{0.75 \cdot l_{sh}}{d_{sh}^4 - d_{shv}^4} + 1.5 \frac{r}{e \cdot h^3} \cdot$$
(4)

Taplin formula – for shafts of a wide variety of engines [4]. The distance between engine masses determined by this formula will be denoted as  $l'_{kol}(12)$ 

$$l_{kol}'(12) = \frac{(l_{k} + 0.15 \cdot d_{k})}{(d_{k}^{4} - d_{kv}^{4})^{2}} \cdot d_{k}^{4} - \frac{l_{sh} + 0.15 \cdot d_{shv}}{(d_{sh}^{4} - d_{shv}^{4})^{2}} \cdot d_{shv}^{4} + \frac{+2e - 0.15(d_{sh} - d_{k})}{h^{4} - d_{shv}^{4}} + \frac{0.065 \cdot d_{k} + 0.58 \cdot e}{e^{2} \cdot h^{3}}r + \frac{0.16}{h \cdot e^{2}}.$$
(5)

#### **Results and discussion**

The obtained results depend on the spatial structure of the crankshaft scheme and its design parameters and may differ by 5-7 % from the experimental data [5]. Therefore, to unify the calculation methods and reduce their complexity, it is proposed to consider the elastic-deformable section of the crankshaft, taking into account its geometric parameters [6; 7].

The formula for determining the reduced length of a compound knee, where the axes of the main and crankpin journals lie in the same plane, will be denoted as  $l'_{kol}(16)$ 

$$l_{kol}^{'}(16) = \left(l_{k} + 0.6\frac{e_{1}}{l_{k}}d_{k}\right) + \left(0.8 \cdot l_{sh} + 0.2\frac{h_{1}}{r}d_{k}\right) \cdot \frac{d_{k}^{4} - d_{kv}^{4}}{d_{sh}^{4} - d_{shv}^{4}} + \left(0.8 \cdot l_{sh} + 0.2\frac{h_{2}}{r}d_{k}\right) \frac{d_{k}^{4} - d_{kv}^{4}}{d_{sh}^{4} - d_{shv}^{4}} + \frac{r\sqrt{r}}{\sqrt{d_{sh}}} \left(\frac{d_{k}^{4} - d_{kv}^{4}}{e_{1} \cdot h_{1}^{3}} + \frac{d_{k}^{4} - d_{kv}^{4}}{e_{2} \cdot h_{2}^{3}}\right).$$
(6)

Let us consider the influence of the design parameters of the crankshaft on the results of its calculations for torsional vibrations, when determining the parameters of an equivalent torsional scheme on the example of a spark six-cylinder four-stroke opposite engine with a nominal power of Ne = 170 kW [8; 9].

The following geometric parameters of the crankshaft of this engine are used as input data:

diameter of the crankshaft main journal  $d_k = 0.045$  m; crankpin journal diameter  $d_{sh} = 0.045$  m; length of the crankshaft main journal  $l_k = 0.026$  m; crankpin journal length  $l_{sh} = 0.026$  m; thickness of the cheek e = 0.008 m; width of the cheek h = 0.1 m; radius of the crank r = 0.0366 m; diameter of the inner shaft cavity  $d_{kv} = 0$ ,  $d_{shv} = 0$ .

For comparison of various formulas the reduced length is considered as a function of the dependence on the diameter of the main journal  $l'_{kol} = f(d_k)$  on the diameter of the crankpin journal  $l'_{kol} = f(d_{sh})$ , on the length of the main journal  $l'_{kol} = f(l_k)$  and the length of the crankpin journal  $l'_{kol} = f(l_{sh})$ . Other parameters are accepted as permanent.

To do this, the range of values in the segment is defined  $d_{sh} = [0.045 - 0.055]$ ,  $d_k = [0.045 - 0.055]$ ,  $l_k = [0.026 - 0.036]$ ,  $l_{sh} = [0.026 - 0.036]$ , in increments 0.001 m.

Fig. 2 shows the effect of changing the diameter of the crankshaft root neck on the reduced length of the equivalent design scheme. According to the figure, the most invariant are the results of calculations using formulas (2), (4) and (6).

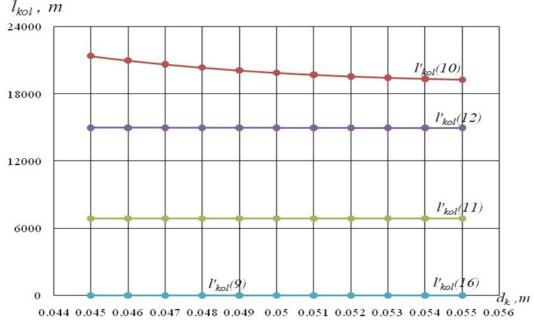


Fig. 2. Influence of the diameter of the main journal on the reduced length

In the future, we will consider the influence of individual parameters for each of the formulas.

Fig. 3 shows a graph comparing the impact of the crankshaft parameters  $d_k$ ,  $d_{sh}$ ,  $l_k$  and  $l_{sh}$  on the value of the reduced length for the Zimanenko formula.

It can be seen from the graph that as the length of the main and crankpin journals increases, the reduced length will increase, and, accordingly, the rigidity of the shaft section will decrease.

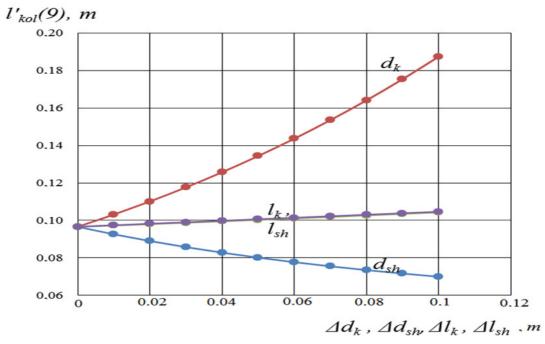


Fig. 3. Influence of design parameters on the reduced length by Zimanenko formula

An increase in the diameter of the crankpin journal leads to a decrease in the reduced length of the shaft section, and, therefore, to an increase in the rigidity of the shaft section. The inverse result gave an increase in the diameter of the main journal – if it increases, the reduced length increases and the stiffness decreases.

Fig. 4 shows a graph comparing the influence of the crankshaft parameters  $d_k$ ,  $d_{sh}$ ,  $l_k$  and  $l_{sh}$  on the value of the reduced length for the formula of the Kolomna plant.

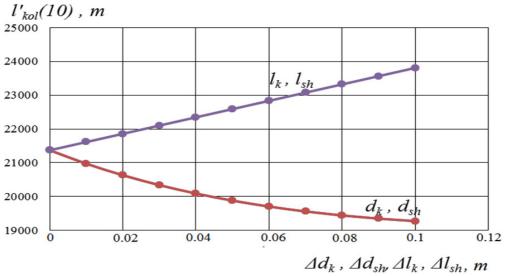


Fig. 4. Influence of design parameters on the reduced length according to the formula of the Kolomna plant

The graph shows that when the length of the main and crankpin journals increases, the reduced length will increase, respectively, the rigidity of the shaft section will decrease. An increase in the diameter of the main and crankpin journal leads to a decrease in the reduced length of the shaft section, and therefore to an increase in the rigidity of the shaft section.

The influence of design parameters on the reduced length according to the Carter formula is shown in Fig. 5.

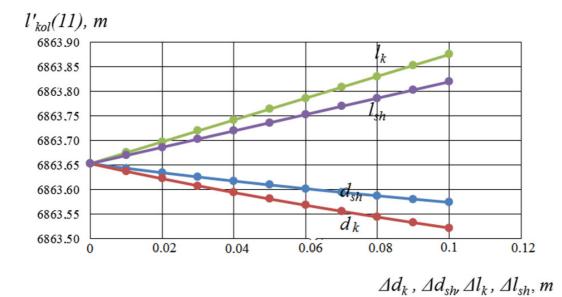
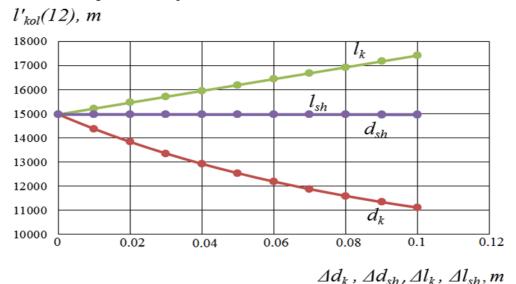
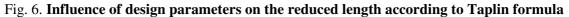


Fig. 5. Influence of design parameters on the reduced length according to the Carter formula

The graph shows that with increasing the length of the main and crankpin journals, the reduced length will increase, respectively, the stiffness of the shaft section will decrease, while increasing the length of the main journal has a stronger effect on reducing the stiffness of the shaft section. The increase in the diameter of the main and crankpin journals reduces the length of the given section of the shaft, and hence to increase the stiffness of the area of the shaft, increasing the diameter of the main journal leads to a greater increase of the stiffness of the section of the shaft.

Fig. 6 shows a graph comparing the impact of the crankshaft parameters  $d_k$ ,  $d_{sh}$ ,  $l_k$  and  $l_{sh}$  on the value of the reduced length for the Taplin formula.





The graph shows that as the length of the main journal increases, the reduced length will increase, respectively, the stiffness of the shaft section will decrease. An increase in the diameter of the crankshaft main journal leads to a decrease in the reduced length of the shaft section, and, therefore, to an increase in the rigidity of the shaft section. At the parameters of  $d_{kv} = 0$ ,  $d_{shv} = 0$ , increase of the crankpin journal length and crankpin journal diameter does not result in special change of reduced length.

The influence of design parameters on the reduced length according to the formula for determining the reduced length of a complex knee is shown in Fig. 7.

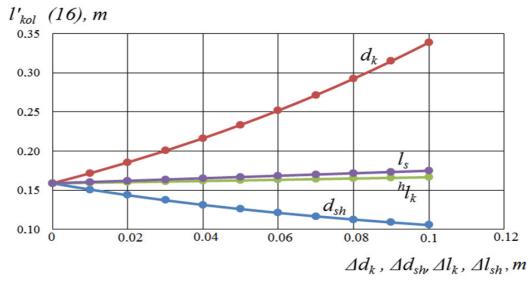


Fig. 7. Influence of design parameters on the reduced length according to the formula for determining the reduced length of a complex knee

The graph shows that when the length of the main and crankpin journals increases, the reduced length will increase, respectively, the stiffness of the shaft section will decrease, and increasing the length of the crankpin journal gives a greater increase in the reduced length. An increase in the diameter of the crankpin journal leads to a decrease in the reduced length of the shaft section, and therefore to an increase in the rigidity of the shaft section. The opposite result was an increase in the diameter of the main journal, with its increase, the reduced length increases, and the stiffness decreases.

## Conclusions

The resulting calculations and graphs show that these formulas were derived for different engines and crankshafts.From most calculations and graphs, it is concluded that an increase in the diameters of the necks and an increase in the overlap of the necks increases the stiffness of the shaft, an increase in the lengths of the necks, on the contrary, reduces the stiffness of the shaft. The values given length closest to reality of the values shown in Zimanenko formula and formula for identification of given length of the complex knee, is the axis of the root and connecting rod journals in one plane. According to the change in the given length, depending on the diameters and lengths of the crankshaft main and crankpin journals, good results were shown by the formulas of the Kolomna plant and the Carter formula.

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